

Al doped graphene: A promising material for hydrogen storage at room temperature

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A promising material for hydrogen storage at room temperature—Al doped graphene is proposed theoretically by using density functional theory calculation. Hydrogen storage capacity of 5.13 wt % is predicted at $T=300$ K and $P=0.1$ GPa with an adsorption energy $E_b = -0.260$ eV/H₂. This is close to the target specified by U.S. Department of Energy with a storage capacity of 6 wt % and a binding energy of -0.2 to -0.4 eV/H₂ at ambient temperature and modest pressure for commercial applications. It is believed that the doped Al alters the electronic structures of both C and H₂. The bands of H₂ overlapping with those of Al and C simultaneously are the underlying mechanism of hydrogen storage capacity enhancement. © 2009 American Institute of Physics. [DOI: 10.1063/1.3103327]

I. INTRODUCTION

In recent years, hydrogen-based fuel systems have been considered to be a highly important topic of research for future energy schemes as hydrogen is a more efficient fuel in comparison to the existing carbonaceous fossil fuels.^{1,2} Despite many recent technological developments in the hydrogen-based fuel systems, it is still an enormous challenge to have safe and efficient reversible hydrogen storage systems at ambient conditions.² One possible way for hydrogen storage is an efficient and controllable adsorption/desorption system. Carbon based materials appear promising for such a purpose. Although several mechanisms of hydrogen storage through both physisorption and chemisorption have been proposed,^{3–7} most of these efforts are far to reach the target of 6 wt % and binding strength of -0.2 to -0.4 eV/H₂ at ambient temperature and modest pressure for commercial applications specified by U.S. Department of Energy (DOE).

With density functional theory (DFT) simulations, it was predicted that a single ethylene molecule can form a stable complex with two transition metals, thus adsorbing ten H₂ molecules and lead to a high storage capacity of ~ 14 wt %.⁸ In addition, the highest H₂ storage capacity of 13 wt % in a fullerene cage with 12 Li atoms capped onto the pentagonal faces was calculated.⁹ This system has average adsorption energy $E_b = -0.075$ eV/H₂. However, all the DFT results are in the ideal condition at the temperature of $T=0$ K; their performances at the DOE specified operation conditions are unclear.

Since carbon nanostructures have high surface areas and thermal stability along with unique mechanical properties, improvement of their adsorption capacity by suitable modification would be of immense interest.^{3–9} Thus, hydrogen

storage using carbon nanostructures is still an important issue and deserves more attention. In this work, the potential of graphene as hydrogen storage materials through doping is investigated. The advantages of graphene are as follows: (1) a large surface for hydrogen adsorption, (2) economical and scalable production,¹⁰ and (3) the strongest material ever measured.¹¹

AlH₃ and related aluminum hydrides as hydrogen storage materials have recently become the focus of renewed interest^{12,13} as their potentially large hydrogen capacity of ~ 10 wt %. These materials are thermodynamically unstable in ambient, but it is kinetically stable without much loss of hydrogen for years. Despite these excellent properties, extremely high pressure (exceeding 2.5 GPa) is required for hydrogen adsorption. While these hydrides possess a small negative enthalpy of formation,¹³ for practical applications, the large hydrogen desorption energy proves impractical. The origin of this energy barrier lies in the rather strong mixed ionic and covalent bonds¹³ formed between Al and H. Thus it is essential to significantly reduce the desorption energy.

There appears another way for Al atoms to store hydrogen, i.e., to further decrease the interaction between Al and H. In this way, the weak chemisorption can be changed into strong physisorption. For hydrogen storage through physisorption, strong interaction between the H₂ molecule and the surfaces along with a large surface area for adsorption is required. The unique characteristics of graphene and Al for hydrogen storage lead to an investigation of the properties of Al doped graphene as a possible hydrogen storage candidate. It would be intriguing to understand the interaction between graphene, Al, and H. In this work, the adsorption behavior of H₂ in Al doped graphene was studied by DFT calculation. In addition, we processed the *ab initio* molecular dynamics (MD) calculation to investigate the effects of temperature and pressure on the corresponding adsorption and desorption behaviors of this system.

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II. CALCULATION METHODOLOGY

All DFT calculations are performed in DMOL3 code.¹⁴ Previous studies^{15,16} have shown that the local density approximation (LDA) prediction of the physisorption energies of H₂ on the surface of graphite and carbon nanotubes is in good agreement with experiments. The reliability of LDA can be ascribed to the following facts.¹⁵ (1) When the electron densities of H₂ and graphene overlap weakly, the non-linearity of the exchange-correlation energy density functional produces an attractive interaction even in the absence of electron density redistribution. (2) The overestimated binding energy by LDA (Refs. 17 and 18) may compensate for the insufficient account of van der Waals interactions.¹⁵ In contrast, DFT calculation using a uniform generalized gradient approximation (GGA) produced a purely repulsive interaction. Using a GGA-PW91 functional, a repulsive interaction between H₂ and a graphene layer and also between H₂ and a (6,6) carbon nanotube was obtained.¹⁹ This contradicts the experimental findings.²⁰ It was noted that LDA calculations well reproduce the empirical interaction potentials between graphitic layers and also in the other graphitic systems for distances near the equilibrium separation although the LDA is not able to reproduce the long-range dispersion interaction.²¹ Therefore, LDA is selected in this work. To ensure that the calculated results are comparable, identical conditions are employed for the isolated H₂ molecules and the graphene and also the adsorbed graphene system. The *k*-point is set to 6 × 6 × 2 for all slabs, which brings out the convergence tolerance of energy of 1.0 × 10⁻⁵ hartree (1 hartree = 27.2114 eV) and that of maximum force is 0.002 hartree/Å.

In the simulation, three-dimensional periodic boundary condition is taken and H–H bond length is set to $l_{\text{H-H}} = 0.74$ Å, which is consistent with the experimental results.²² The graphene used in our simulation consists of a single layer of 3 × 3 supercell with a vacuum width of 12 Å to minimize the interlayer interaction. Increasing the vacuum width will greatly increase the computation expense although it has only negligible consequence on the results obtained. All atoms are allowed to relax in all energy calculations. The adsorption energy E_b between the H₂ gas molecule and graphene is defined as

$$E_b = E_{\text{H}_2+\text{graphene}} - (E_{\text{graphene}} + E_{\text{H}_2}), \quad (1)$$

where the subscripts H₂+graphene, graphene, and H₂ denote the adsorbed system, isolated graphene, and H₂ molecules, respectively.

For the Al doped graphene, the concentration of Al is 12.5 at. % with the additional constraint that there is only one Al atom per graphene hexagonal ring (Fig. 1) to avoid Al atoms clustering on graphene.²³ For H₂ adsorption on the Al doped graphene, there are four top sites of T1, T2, T3 and T4, three bridge sites of B1, B2, and B3, and two center sites of C1 and C2, as shown in Fig. 1. (In this figure, a larger simulation cell is given in order to better display the different adsorption sites on the Al doped graphene. Figure 2 reflects the actual simulation cell size.) At each adsorption site, there are two highly symmetrical adsorption configurations,

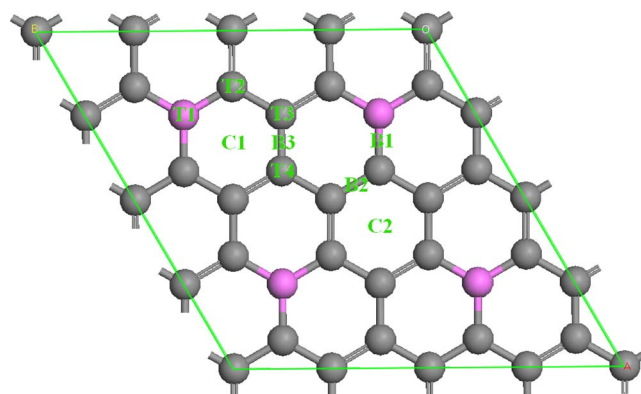


FIG. 1. (Color online) Nine different adsorption sites on the Al doped graphene. The gray and pink balls are, respectively, C and Al atoms.

namely, H₂ molecule resides parallel or perpendicular to the graphene surface. Therefore, a total of 18 adsorption configurations for H₂ on the Al doped graphene is present.

Due to the periodicity of H₂ adsorbed in intrinsic graphene or Al-doped-graphene systems, we have selected the unit cell with the following conditions: eight C atoms and one H₂, or seven C atoms, one Al atom, and one H₂ (see Fig. 2). If we place a H₂ at any location of the cell, the distance from this H₂ to other H₂ molecules in the nearest cells is 4.920 Å. This large separation, compared to the bond length of H₂ (0.740 Å), would ensure that there is no interaction between H₂ molecules in the different cells.²⁴

To calculate the H₂ adsorption capability of Al doped graphene at room temperature and modest pressure, we performed *ab initio* MD calculation with Cambridge sequential total energy package (CASTEP) code based on the structure obtained by DFT above, which utilizes plane-wave pseudo-potential to perform the first principles quantum mechanics calculations.²⁵ LDA with the Ceperley–Alder–Perdew–Zunger function^{26,27} was employed as exchange-correlation

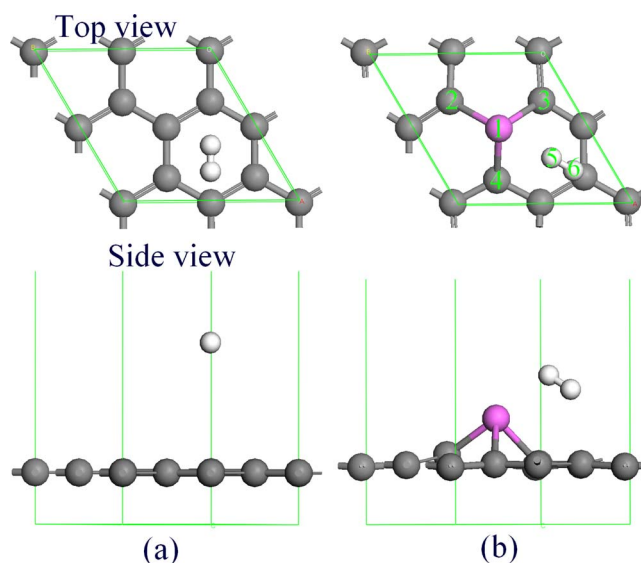


FIG. 2. (Color online) The favorite adsorption configurations with one H₂ molecule adsorbed in (a) intrinsic graphene and in (b) Al doped graphene. The gray and pink balls have the same meaning in Fig. 1, and the white balls are H atoms.

TABLE I. Summary of results for H₂ adsorption on intrinsic graphene and Al doped graphene on different adsorption sites. For H₂ adsorption on intrinsic graphene, there are six different adsorption sites as listed in the table. For H₂ adsorption on Al doped graphene, there are 18 different adsorption configurations, as shown in Fig. 1.

Initial binding configuration		Intrinsic graphene		Al doped graphene		
		E_b (eV)	d (Å) ^a	E_b (eV)	l (Å) ^b	d (Å) ^a
H ₂ //graphene	T1	-0.136	2.845	-0.209	2.762	
	T2			-0.34	2.526	2.682
	T3			-0.407	2.588	2.486
	T4			-0.361	2.942	2.537
	B1	-0.139	2.817	-0.21	2.757	
	B2			-0.411	2.527	2.575
	B3			-0.411	2.506	2.563
	C1	-0.159	2.635	-0.427	2.083	2.073
	C2			-0.188		2.657
H ₂ ⊥graphene	T1	-0.141	2.615	-0.153	2.622	
	T2			-0.284	2.427	2.749
	T3			-0.406	2.367	2.524
	T4			-0.33	2.976	2.179
	B1	-0.142	2.620	-0.206	2.271	3.732
	B2			-0.412	2.468	2.595
	B3			-0.426	3.196	2.074
	C1	-0.148	2.425	-0.426	2.092	2.104
	C2			-0.24	3.117	2.468

^aDistance between H₂ molecule and graphene or Al-doped-graphene layer.

^bDistance between Al and H₂.

functions, cutoff energy $E_c=280$ eV, and k -points is $6 \times 6 \times 2$. In principle, E_c increases until the calculated total energy converges within the required tolerance. $dE_{\text{tot}}/d \ln E_c$ is the parameter used to evaluate the accuracy of the calculation, where E_{tot} is the total energy of the system. The software can calculate $dE_{\text{tot}}/d \ln E_c$ value automatically. In general, $dE_{\text{tot}}/d \ln E_c=0.1$ eV/atom is sufficient for the most calculations. The values of k -points are increased until the calculated energy converges within the required tolerance, where the k -points sample the irreducible wedge of the Brillouin zone. In this work, the k -points of $6 \times 6 \times 2$ for all slabs have the energy convergence tolerance of 1.0×10^{-6} eV/atom. Such energy tolerance is small enough to ensure establishment of the actual equilibrium structure.

Each MD simulation was performed in NPT statistical ensemble, i.e., constant numbers of atoms N , pressure P , and T , with $T=300$ K and $P=0.0001-1$ GPa. A time step of 1 fs was selected and simulation time t at a particular T was 2.5 ps where the total energy fluctuation was in the range of 0.01%. The same t was selected for H₂S dissociation on the Fe(110) surface.²⁸ A Verlet algorithm²⁹ was used to integrate the equations of motion, with T controlled by algorithm of Nose,³⁰ and P was controlled according to the Parrinello–Raham algorithm.³¹ A key parameter in the integration algorithms is the integration time step. A common rule of thumb used to set the time step is that the highest frequency vibration should be sampled between 10 and 20 times in 1 cycle. In this system, the frequency is in the order of 10^{13} Hz;³² the time step is thus set as 1 fs within a reasonable range.

III. RESULTS AND DISCUSSION

After geometry relaxation, E_b values and the corresponding structure parameters of the six adsorption configurations for H₂ adsorbed in the intrinsic graphene are listed in Table I. It was found that the most favorable configuration is H₂ adsorbed on the center site of the carbon ring with $E_b=-0.159$ eV as shown in Fig. 2(a) and the distance between H₂ and the graphene is $d=2.635$ Å. The results are consistent with other reported results of $E_b=-0.133$ eV and $d \approx 2.8$ Å.¹⁶ The small magnitude of E_b shows that the system is in the weak physisorption region. It indicates that the intrinsic graphene is not suitable for hydrogen storage under the postulated operating conditions.

For the adsorption of H₂ in the Al doped graphene, the corresponding results are also listed in Table I. As can be seen from Table I, the most favorable position with $E_b=-0.427$ eV for the H₂ molecule is shown in Fig. 2(b). The distance between H₂ and the doped Al is $l=2.083$ Å while that between H₂ and carbon layer is $d=2.073$ Å. As seen from Table I, the interaction reaches the strongest when both l and d are minimized. The adsorption of H₂ in the Al doped graphene is larger than that in other systems, such as $E_b=-0.41$ eV/H₂ in the Ti–C₂H₄-graphene system⁸ and $E_b=-0.08$ eV/H₂ in 12-Li-doped fullerene.⁹ However, this still belongs to the physisorption system as the long distance between the doped graphene and the adsorbed H₂. Therefore, this strong physisorption interaction would be ideal for hydrogen storage, which can adsorb more H₂ molecules.

To understand the enhancement effect of the doped Al on

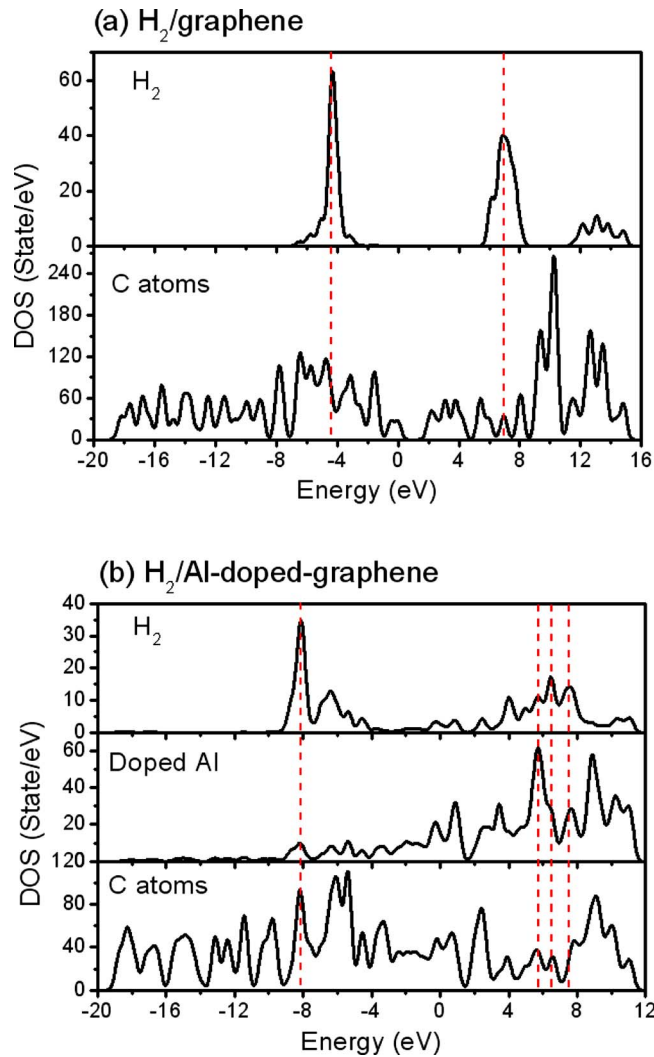


FIG. 3. (Color online) The PDOS of adsorbed H_2 , doped Al, and graphene in both the H_2 /graphene and H_2 /Al-doped-graphene systems, as shown in panels (a) and (b), respectively. Fermi level is set to 0.

the H_2 adsorption, the projected electronic density of states (PDOS) of the adsorbed H_2 , the doped Al, and the C atoms in both H_2 /graphene and H_2 /Al-doped-graphene systems are plotted and shown in Fig. 3. Figure 3(a) shows the PDOS of H_2 /graphene system. The main peaks of H_2 are located at -4.37 and 6.92 eV. However, the main peaks of intrinsic graphene are located between 9 and 13 eV. Therefore, the interaction between H_2 molecule and the intrinsic graphene is very weak because of nonoverlapping of electrons in these substances, where E_b is small. On the other hand, for the H_2 /Al-doped-graphene system shown in Fig. 3(b), the main peaks of H_2 are located at -8.15 , 5.74 , 6.52 , and 7.51 eV, respectively. The bands of H_2 interact with both the doped Al and the C atoms simultaneously at the positions indicated by the dashed lines, showing a strong interaction between H_2 and the Al doped graphene where E_b is the largest. In addition, the doped Al changes the electronic structures of both H_2 and the graphene, and both their PDOSs shift toward the lower energy. This suggests that the H_2 /Al-doped-graphene configuration is a much more stable system.

Table II shows the charge distribution in both the H_2 /graphene and H_2 /Al-doped-graphene systems using

TABLE II. Charges of atoms in H_2 adsorbed in graphene system as well as charge transfer Q between graphene and H_2 molecule obtained by Mulliken analysis. The unit of the atom charge is one electron charge e , which is elided here for clarity.

Atom	Intrinsic graphene	Al doped graphene
Al1 (C1)	0.001	0.292
C2	-0.002	-0.228
C3	0	-0.193
C4	0	-0.193
H5	-0.001	-0.001
H6	-0.001	0.021
Q	-0.002	0.019

Mulliken analysis. Before and after H_2 adsorption, the charge variation for the former is little while it is significant for the latter. In addition, H6 has much more positive charge than H5. Thus, the interaction between H_2 and the Al doped graphene is mainly achieved through H6. The interaction between the band at the location of the highest peak of PDOS plot of H_2 and that of C atoms implies a strong interaction between the H_2 and C atoms, as shown in Fig. 3(b).

The illustrations of electron density distribution for the H_2 /graphene and H_2 /Al-doped-graphene systems are shown in Fig. 4. In the system of H_2 /graphene [Fig. 4(a)], no electron exists in the region between H_2 and C layer while some electrons appear in the region among H_2 , Al atom, and C layer in the system of H_2 /Al-doped-graphene [Fig. 4(b)]. This supports the notion that the H_2 /Al-doped graphene possesses a much stronger H_2 adsorption ability.

After understanding the mechanism of the enhancement for H_2 adsorption in the Al doped graphene, it is important to determine how much H_2 molecules can be adsorbed on the 3×3 layer surface. We constructed an adsorption configuration with three H_2 molecules adsorbed in the three favorable C1 adsorption positions on the top side of the doped system. After geometry relaxation, the atomic structure is shown in Fig. 5(a). It has $E_b = -0.303$ eV/ H_2 , which satisfies the requirement of $E_b = -0.20$ to -0.40 eV/ H_2 at room temperature³⁻⁶ set by DOE although the value of 5.1 wt % of H_2 adsorbed is slightly below the DOE's 6 wt % target.

In order to understand the effect of the adsorbed H_2 molecule number on the E_b , the configuration with six H_2 molecules adsorbed in the Al doped graphene in the favorable C1 adsorption positions on both sides was calculated. It is found that $E_b = -0.164$ eV/ H_2 , which is much smaller than

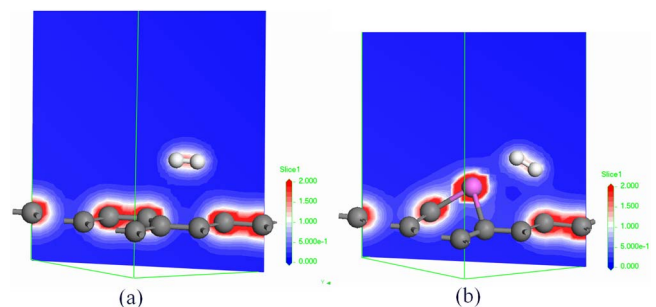


FIG. 4. (Color online) Electron density distributions in the H_2 /graphene [panel (a)] and H_2 /Al-doped-graphene [panel (b)] systems.

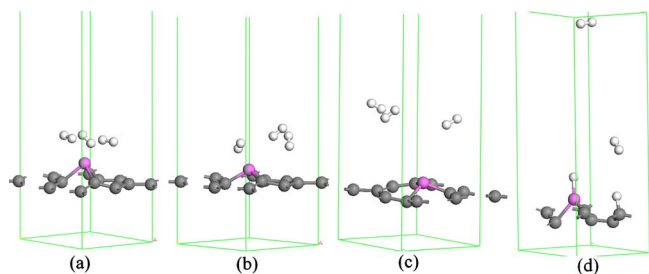


FIG. 5. (Color online) Atomic configurations of three H₂/Al-doped-graphene system at different temperatures and pressures. (a) In the ideal condition with $T=0$ K, (b) in the condition with $T=300$ K and $P=0.1$ GPa, (c) in the condition with $T=300$ K and $P=0.0001$ GPa, and (d) in the condition with $T=300$ K and $P=1$ GPa.

the E_b for the above case where the Al doped graphene adsorbed three H₂ on one side of graphene. In addition, the adsorption with eight H₂ molecules in the Al doped graphene was also calculated, and it is found that two H₂ molecules were released. In other words, the interaction between H₂ molecules would weaken the adsorption and the saturated number of H₂ molecules adsorption is 6. Note that E_b for the cases of three H₂ and six H₂ are, respectively, -0.303 and -0.164 eV/H₂, which is about twice for the case of three H₂ compared with the case of six H₂. This is because H₂ molecules were very weakly adsorbed below the graphene layer where the doped Al atom locates above the graphene layer.

It is well known that increasing pressure (P) and decreasing temperature (T) enhance the capacity of hydrogen storage. Thus, most studied systems are either under high P or at very low T ,²⁰ which may not be viable for mobile applications. For example, it has been reported that purified single wall carbon nanotubes (SWNTs) has a storage capacity of 8 wt % at 80 K with a hydrogen pressure of 13 MPa (Ref. 33) but has only a much lower hydrogen storage capacity of 2.3 wt % at 77 K.³⁴ The hydrogen storage capacities in other carbon related materials, such as activated carbon (AC), single walled carbon nanohorn, SWNTs, and graphite nanofibers, were also reported.³⁵ Although the AC had a capacity of 5.7 wt % at 77 K with $P=3$ MPa, its capacity is $<1\%$ at 300 K.³⁵ Recent experimental results demonstrated that the intrinsic graphene has hydrogen storage capacity of 1.7 wt % under 1 atm at 77 K and of 3 wt % under 100 atm at 298 K.³⁶ Thus, to meet the DOE target, it is necessary to study the adsorption and desorption behaviors of H₂ in the Al doped graphene at $T=300$ K with different P . Therefore, the adsorption behaviors of three H₂/Al-doped-graphene and six H₂/Al-doped-graphene systems were calculated under 0.0001, 0.01, 0.1, and 1 GPa using *ab initio* MD simulation. For both the three H₂/Al-doped-graphene and six H₂/Al-doped-graphene systems, we found that all H₂ molecules were released at 0.0001 GPa [Fig. 5(c)]. However, there was only one H₂ molecule adsorbed in both the systems at 0.01 GPa, while the structure of the doped graphene was completely destroyed with H and Al forming covalent bond at 1 GPa [Fig. 5(d)]. When $P=0.1$ GPa, there are three H₂ left on the top side of the two Al doped systems [Fig. 5(b)]. Therefore, the Al doped graphene for hydrogen storage capacity at room temperature

and 0.1 GPa is 5.13 wt % with $E_b=-0.260$ eV/H₂, satisfying the requirements of actual application. In addition, all the adsorbed H₂ molecules can be released when $P=0.0001$ GPa.

IV. CONCLUSION

In conclusion, the adsorption behaviors of H₂ in the intrinsic and Al doped graphene were studied using DFT. It is found that the physisorption of H₂ is greatly enhanced by doping Al into graphene. The doped Al varies the electronic structures of both C and H₂, causing the bands of H₂ overlapping with those of Al and C simultaneously. It induces an intensive interaction between H₂ and the Al doped graphene. This was also demonstrated by the electron density distribution. In order to understand the temperature and pressure effects on the H₂ adsorption behavior for actual application, *ab initio* MD calculations for the H₂/Al-doped-graphene system were processed. It is found that the system has 5.13 wt % hydrogen storage ability at $T=300$ K with $P=0.1$ GPa. Therefore, the Al doped graphene would be a promising hydrogen storage material owing to the strong interaction between H₂ and the Al doped graphene.

ACKNOWLEDGMENTS

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